

Solución

$$\text{a) } \int \frac{x^4 - 3x}{x^2 - 1} dx = \frac{x^3}{3} + x - \ln(x-1) - 2\ln(x+1) + C$$

$$\text{b) } \int x \ln(x+1) dx = \frac{x^2}{2} \ln(1+x) - \frac{x^2}{4} + \frac{x}{2} - \frac{1}{2} \ln(1+x) + C$$

$$\text{c) } \int (5x-4)^7 dx = \frac{(5x-4)^8}{40} + C$$

$$\text{d) } \int \frac{x^3}{3-5x^4} dx = -\frac{1}{20} \ln(3-5x^4) + C$$

$$\text{e) } \int \frac{\sqrt{x-1}}{x} dx = 2\sqrt{x-1} - 2 \operatorname{arctg} \sqrt{x-1} + C$$

$$\text{f) } \int \frac{(x^2 - 5x + 4) dx}{x^3 + 2x^2 - 15x} = -\frac{4}{15} \ln x - \frac{1}{12} \ln(x-3) + \frac{27}{20} \ln(x+5) + C$$

$$\text{g) } \int 5e^{4x} dx = \frac{5}{4} e^{4x} + C$$

$$\text{h) } \int \frac{x-1}{x-2x^2} dx = \frac{1}{2} \ln(1-2x) - \ln x + C$$

$$\text{i) } \int \frac{e^x + 1}{e^x + x} dx = \ln(e^x + x) + C$$

$$\text{j) } \int \left(2 \sin 3x + 3 \cos \frac{x}{2} \right) dx = -\frac{2}{3} \cos 3x + 6 \sin \frac{x}{2} + C$$

$$\text{k) } \int (x+1) \sin 2x dx = -\frac{1}{2} (x+1) \cos 2x + \frac{1}{4} \sin 2x + C$$

$$\text{l) } \int x^2 e^{3x} dx = \left(\frac{x^2}{3} - \frac{2x}{9} + \frac{2}{27} \right) e^{3x} + C$$

$$\text{ll) } \int \frac{x+3}{x^2-2x+1} dx = \ln(x-1) - \frac{4}{x-1} + C$$